

Communication

# Resolution and sensitivity aspects of ultrafast $J$ -resolved 2D NMR spectra

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## Abstract

Recent ultrafast techniques enable  $n$ D NMR spectra to be obtained in a single scan. However, resolution enhancement in the ultrafast domain leads to important sensitivity losses and lineshape distortions. In order to understand better resolution and spatial encoding aspects of continuous phase-encoding schemes, a theoretical and experimental comparison of different excitation patterns is carried out. Molecular diffusion appears to be the main cause of signal-to-noise ratio decrease, and a multi-echo excitation scheme is proposed to limit its effects when a good resolution is needed. Results obtained on 2D  $J$ -resolved spectra are presented.

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**Keywords:** Ultrafast 2D NMR;  $J$ -resolved spectroscopy; Resolution enhancement; Signal-to-noise ratio; Molecular diffusion

## 1. Introduction

The introduction of two-dimensional (2D) spectroscopy [1,2] is one of the most significant advances in the evolution of nuclear magnetic resonance (NMR) techniques. 2D NMR is used in a wide range of applications, from the study of chemical structures and dynamics to pharmaceutical and medical applications. However, it suffers from long acquisition times due to the necessary collection of numerous  $t_1$  increments to obtain spectra with a good resolution.

Recently, a method based on ultrafast imaging techniques was proposed by Frydman and co-workers [3,4], enabling the acquisition of 2D NMR spectra within a single scan. In this so-called “ultrafast 2D NMR” technique, the usual  $t_1$  encoding is replaced by a spatial encoding, which is decoded during a detection period by an echo planar imaging (EPI) scheme [5]. However, the discrete encoding mode initially proposed suffers from practical drawbacks as it requires fast gradient switching carefully

synchronized with RF irradiation. Moreover, it leads to the appearance of undesirable “ghost peaks” in the indirect domain [6]. To deal with these limitations, a continuous encoding scheme was proposed by Shrot et al. [7], using a pair of continuously frequency-swept pulses applied during a bipolar gradient. Unfortunately, this method involves an amplitude modulation which is incompatible with phase-modulated techniques such as COSY [1] or  $J$ -resolved spectroscopy [8]. Different alternatives were then proposed [9–11] to obtain a phase-modulated encoding in order to circumvent these limitations.

Based on these continuous phase-modulated excitation schemes, we have recently proposed [12] a modification of the acquisition scheme to obtain  $J$ -resolved spectra where coupling constants are encoded along the direct  $v_2$  domain. This scheme was coupled to both Pelupessy's [11] and Tal's [9] excitation patterns. In this study, it appeared that the resolution along the  $k/v_1$  axis was quite disappointing compared to conventional 2D spectra. Moreover, resolution seemed to depend on the excitation scheme and it appeared impossible to improve it without a dramatic decrease of the signal-to-noise ratio.

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In the present paper, the approach of resolution and spatial encoding is rationalized in order to compare the different excitation schemes under similar conditions. An improvement of spatial encoding based on multiple-echoes is proposed, which allows increasing resolution while limiting signal-to-noise losses due to molecular diffusion effects. Results are applied to  $J$ -resolved spectroscopy.

## 2. Results and discussion

### 2.1. Comparison of different continuous phase-encoding schemes

The excitation scheme proposed by Pelupessy [11] and applied to  $J$ -resolved spectroscopy [12] is described in Fig. 1a. It starts with a  $90^\circ$  non-selective pulse, followed by a  $180^\circ$  chirp pulse of duration  $D^\pi$  with a linear frequency ramp applied during a magnetic field gradient  $+G_e^\pi$ . It is followed by an identical pulse applied during an inverted gradient  $-G_e^\pi$ . At the end of the first  $180^\circ$  pulse, it can be shown that the phase evolution of the system possesses constant, linear and quadratic terms, according to:

$$\phi_\pi = -\frac{D^\pi \Omega_1^2}{\gamma_e G_e^\pi L} - \frac{\gamma_e G_e^\pi L D^\pi}{4} - \frac{2D^\pi \Omega_1 z}{L} - \frac{D^\pi \gamma_e G_e^\pi z^2}{L} \quad (1)$$

where  $L$  is the excited height of the sample. In this expression we suppose that the frequency range of the chirp pulse is approximately adjusted to the one induced by the gradient,  $\gamma_e G_e^\pi L$ . The quadratic term prevents the formation of echo peaks in the indirect domain; however it is cancelled by the second  $180^\circ$  pulse, as well as the constant term. At

the end of the excitation scheme, the phase evolution is given by

$$\phi_P^0 = \frac{4D^\pi \Omega_1 z}{L} \quad (2)$$

which possesses the linear dependence in  $\Omega_1 z$  required by ultrafast 2D NMR. There is no constant term in Eq. (2); one could then expect that a spoiler prior to acquisition is not necessary. However, the application of a short gradient can be useful to compensate for experimental errors or to set the echoes at the desired position.

Tal et al. [9] proposed another method leading to a continuous phase encoding, described in Fig. 1b. It consists of a  $90^\circ$  continuous excitation performed by a chirp pulse of duration  $D^{\pi/2}$  with a linear frequency ramp, applied during a positive gradient  $G_e^{\pi/2}$ . This excitation is immediately followed by a  $180^\circ$  chirp pulse of duration  $D^\pi$ , applied during a positive magnetic field gradient  $G_e^\pi$ . At the end of the  $90^\circ$  pulse, the phase evolution is given by

$$\phi^{\pi/2} = \frac{D^{\pi/2}}{2} \left( \Omega_1 - \frac{\Omega_1^2}{\gamma_e G_e^{\pi/2} L} - \frac{\gamma_e G_e^{\pi/2} L}{4} \right) + \frac{D^{\pi/2}}{L} \left[ \frac{\gamma_e G_e^{\pi/2} L}{2} - \Omega_1 \right] z - \frac{\gamma_e G_e^{\pi/2} D^{\pi/2}}{2L} z^2 \quad (3)$$

The quadratic term is removed by the  $180^\circ$  pulse when the condition

$$D^{\pi/2} G_e^{\pi/2} = 2D^\pi G_e^\pi \quad (4)$$

is respected [9]. Under this condition, the  $z$ -dependence of the phase evolution at the end of the encoding process can be written:

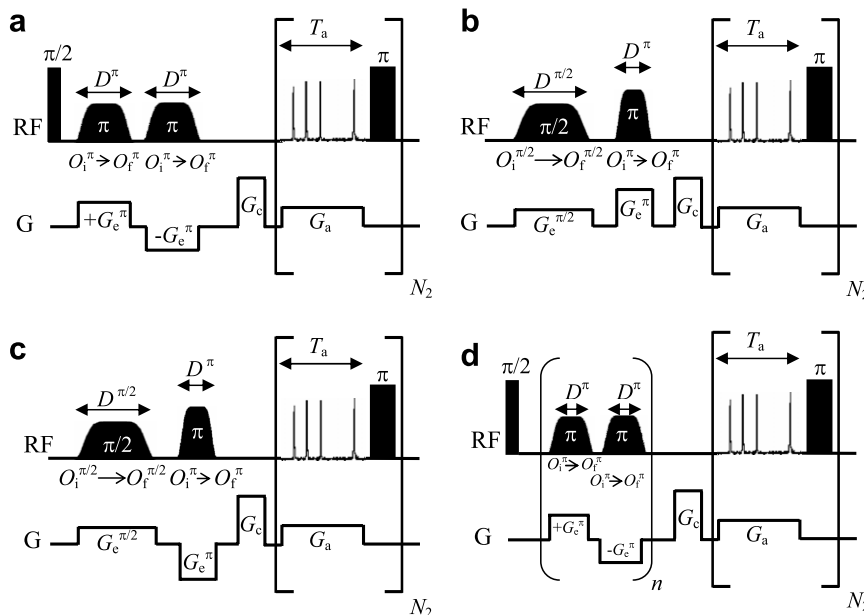


Fig. 1. Pulse sequences for the acquisition of ultrafast 2D  $J$ -resolved spectra, using phase-modulated encoding schemes proposed by Pelupessy (a) and Tal et al. (b), or using Tal's scheme with inverted  $G_e^\pi$  gradient (c). (d) Multiple-echo excitation scheme designed to limit diffusion effects. The  $G_c$  gradient prior to acquisition is adjusted to set the middle of the chemical shift range in the middle of the detection period  $T_a$ . The  $180^\circ$  pulse phase is alternated ( $y, y, -y, -y$ ) to avoid undesirable stimulated echoes.

$$\phi_T^0(z) = \left[ -\frac{D^{\pi/2}\gamma_e G_e^{\pi/2}}{2} + \frac{D^{\pi/2}}{L} \left( 1 - \frac{G_e^{\pi/2}}{G_e^\pi} \right) \Omega_1 \right] \cdot z \quad (5)$$

assuming that the frequency range of each chirp pulse matches the one of the corresponding gradient. In Eq. (5), the  $\Omega_1$ -independent contribution is an offset that can be easily compensated by an appropriate gradient  $G_e$  prior to acquisition. The evolution phase also contains a  $z$ -independent term which leads to a first-order phase distortion. Spectra are represented in magnitude mode to avoid dealing with this distortion.

A slightly different version of Tal's encoding pattern was suggested by Andersen and Kockenberger [10]. Here, the gradient  $G_e^\pi$  applied during the  $180^\circ$  pulse is inverted (Fig. 1c). When calculating the phase  $\phi_T^0(z)$  at the end of such a scheme, we obtain the following expression:

$$\begin{aligned} \phi_T^0 = & \left[ -D^\pi \left( \frac{\Omega_1^2}{\gamma_e G_e^\pi L} + \frac{\gamma_e G_e^\pi L}{4} \right) \right. \\ & \left. - \frac{D^{\pi/2}}{2} \left( \Omega_1 - \frac{\Omega_1^2}{\gamma_e G_e^{\pi/2} L} - \frac{\gamma_e G_e^{\pi/2} L}{4} \right) \right] \\ & + \left[ -\frac{D^{\pi/2}\gamma_e G_e^{\pi/2}}{2} + (D^{\pi/2} + 2D^\pi) \frac{\Omega_1}{L} \right] \cdot z \\ & + \gamma_e \left[ \frac{D^{\pi/2} G_e^{\pi/2} - 2D^\pi G_e^\pi}{2L} \right] \cdot z^2 \end{aligned} \quad (6)$$

When condition (4) is fulfilled, the quadratic term is cancelled and the  $z$ -dependence of the phase evolution at the end of the encoding process can be written:

$$\phi_T^0(z) = \left[ -\frac{D^{\pi/2}\gamma_e G_e^{\pi/2}}{2} + \frac{D^{\pi/2}}{L} \left( 1 + \frac{G_e^{\pi/2}}{G_e^\pi} \right) \Omega_1 \right] \cdot z \quad (7)$$

The evolution phase also contains a  $z$ -independent term which leads to a first-order phase distortion that can be eliminated using magnitude mode. Contrary to Andersen and Kockenberger's recommendation [10], it appears that the sweep direction of the  $180^\circ$  pulse should not be reversed, as the quadratic term could not be cancelled in this case. Eq. (7) is very similar to Eq. (5), except that factor  $(1 - G_e^{\pi/2}/G_e^\pi)$  is replaced by  $(1 + G_e^{\pi/2}/G_e^\pi)$ .

At this stage, it appears necessary to define parameters that would help us to compare the three excitation schemes under the same conditions. To perform this comparison, we shall call  $T_e$  the average time spent by the magnetization in the transverse plane. The value of  $T_e$  for each encoding scheme is given in Table 1. Encoding schemes should be compared with identical  $T_e$  values to make sure they have the same dependence on transverse relaxation. We will also compare the spatio-temporal encoding constants  $C$ , which is the  $\Omega_1 z$  dependence of the phase evolution at the end of the encoding process [3]. For each scheme,  $C$  is expressed as a function of  $T_e$  and the resulting expression is given in Table 1.

It clearly appears that for identical  $T_e$  values, the spatial encoding level is higher with Pelupessy's excitation scheme

Table 1

Relevant parameters (average time in transverse plane  $T_e$  and spatio-temporal encoding level  $C$ ) for different continuous encoding schemes

Encoding scheme	$T_e$	$C$
Pelupessy	$2D^\pi$	$\frac{2T_e}{L}$
Tal	$\frac{D^{\pi/2}}{2} + D^\pi$	$\frac{2T_e}{L} \cdot \frac{1 - G_e^{\pi/2}/G_e^\pi}{1 + G_e^{\pi/2}/G_e^\pi}$
Tal with inverted $G_e^\pi$ gradient	$\frac{D^{\pi/2}}{2} + D^\pi$	$\frac{2T_e}{L}$

The frequency range for each WURST pulse is supposed to match approximately the one induced by the corresponding gradient and for the two last schemes, condition (4) is supposed to be fulfilled.

than with Tal's, because the latter is modulated by the  $G_e^{\pi/2}/G_e^\pi$  ratio. However, Tal's scheme with inverted  $G_e^\pi$  gradient leads to the same encoding constant than Pelupessy's, as it does not depend any more on the gradient ratio for a given  $T_e$  value.

It is also interesting to compare the resolution of the different methods, which can be evaluated by the half-height width  $\delta v^{1/2}$  in the ultrafast  $k/v_1$  dimension.  $\delta v^{1/2}$  can be calculated by Eq. (8):

$$\delta v^{1/2} = \frac{\delta \tau^{1/2}}{\Delta \tau_a} \cdot \Delta v \quad (8)$$

In this expression,  $\Delta \tau_a$  is the time between two echoes detected by the same acquisition gradient, corresponding to two peaks separated by  $\Delta v$ ;  $\delta \tau^{1/2}$  is the temporal half-height width of the echo peaks. To calculate this expression for a given encoding scheme, it should be reminded that the echo appears at the exact moment  $\tau_a$  when the dephasing induced by the acquisition gradient,  $\gamma_a G_a \tau_a z$ , compensates for the  $z$ -dependent term of the phase at the beginning of the detection gradient,  $\phi^0(z)$  [3]. Thus, the echo temporal position in the ultrafast dimension is given by Eq. (9):

$$\tau_a = \frac{\phi^0(z)}{\gamma_a G_a z} = \frac{C \Omega}{\gamma_a G_a} \quad (9)$$

and the duration  $\Delta \tau_a$  separating two echoes can be calculated by:

$$\Delta \tau_a = \frac{C}{\gamma_a G_a} \cdot 2\pi \Delta v \quad (10)$$

Moreover, if the lineshape is approximated to a Sine function [13], the temporal half-height width  $\delta \tau^{1/2}$  is approximately  $7.58/(\gamma_a G_a L)$ . Finally, it can be shown that  $\delta v^{1/2}$  is inversely proportional to the spatio-temporal encoding constant  $C$  according to:

$$\delta v^{1/2} \approx \frac{1.21}{LC} \quad (11)$$

Eq. (11) shows that  $C$  is sufficient to characterize resolution. The higher  $C$  is, the better resolution is. The  $C$  values obtained for both encoding schemes (Table 1) demonstrate that the highest resolution is obtained for Pelupessy's scheme and for Tal's scheme with inverted  $G_e^\pi$  gradient.

As a conclusion, Tal's scheme using inverted gradient should theoretically lead to the same result as Pelupessy's

scheme. To check this assessment, we performed  $J$ -resolved ultrafast experiments using both excitation schemes with the same  $T_e$  (60 ms) and same gradient amplitudes. For Tal's inverted scheme, the  $G_e^{\pi/2}/G_e^\pi$  ratio was initially set to 1. The spectra obtained on a 3-ethyl bromopropionate sample are presented in Fig. 2. As expected, both spectra almost have the same resolution in the ultrafast dimension. The half-height width, measured on the 2D ultrafast spectrum projection along  $k/v_1$  axis, is  $17 \pm 1$  Hz for Pelupessy's scheme (Fig. 2a) and  $20 \pm 1$  Hz for Tal's inverted scheme (Fig. 2b). We also varied the  $G_e^{\pi/2}/G_e^\pi$  ratio for Tal's inverted scheme and we do not observe significant differences for half-height widths, which confirms that the resolution does not depend on the gradient ratio. However, in these experiments, measured  $\delta v^{1/2}$  values are higher than the ones predicted by Eq. (11) (10 Hz for  $T_e = 60$  ms), which may be due to experimental parameter variations.

In spite of similar resolutions for both schemes, the signal-to-noise ratio is higher for Pelupessy's excitation scheme ( $S/N = 140 \pm 15$ , measured on the highest peak of the quadruplet) than for Tal's ( $S/N = 70 \pm 30$ ). Moreover, the peak intensities on the projection seem more distorted for Tal's scheme (Fig. 2b). The three peaks at 2.9, 3.6 and 4.2 ppm are expected to have the same intensities as they each correspond to two protons, which is clearly not the case here. However, it should be noted that the time  $T_e$  spent by magnetizations in the transverse plane is an average value for Tal's scheme whereas it is an exact value for Pelupessy's, as in the second case all magnetizations are flipped in  $xy$  plane at the same time.

Because of these intensity distortions, we were not able to use the same cross-section levels in Fig. 2a and b in order

to obtain a correct definition of the weakest multiplets. This explains why 2D peaks look different in Fig. 2 in spite of similar resolutions.

It should also be noted that Tal's scheme appears much more difficult to set than Pelupessy's, because the  $90^\circ$  pulse must be carefully calibrated to obtain an accurate  $\pi/2$  excitation with an adiabaticity parameter of  $0.068$  [14], and also because the  $G_e^\pi$  value must be adjusted to obtain the sharpest echo peaks, as noticed by Tal et al. [9]. Consequently, Pelupessy's scheme appears easier to implement in routine procedures.

## 2.2. Resolution versus sensitivity

According to the results presented in Table 1, resolution could be improved by simply increasing the value of  $T_e$ . To verify this assessment, we increased the duration of the excitation period ( $T_e = 120$  ms) for Pelupessy's excitation scheme [11], by doubling the duration of the  $180^\circ$  excitation pulses, which should theoretically lead to  $\delta v^{1/2} = 5$  Hz, according to Eq. (11). The corresponding spectrum is shown in Fig. 3a. The expected resolution improvement is observed (half-height width decreased to  $13 \pm 1$  Hz) even though  $\delta v^{1/2}$  is higher than the expected value. However, the signal-to-noise ratio dramatically decreases ( $S/N = 15 \pm 5$  for the highest peak of the quadruplet). Moreover, the projection shows important lineshape distortions, particularly for the triplet at 1.3 ppm. This is probably due to an incomplete refocusing of corresponding magnetizations.  $T_e$  was also increased to 120 ms for Tal's scheme and the same evolution was observed. Sensitivity decrease was too important to be able to measure  $S/N$  ratio and resolution.

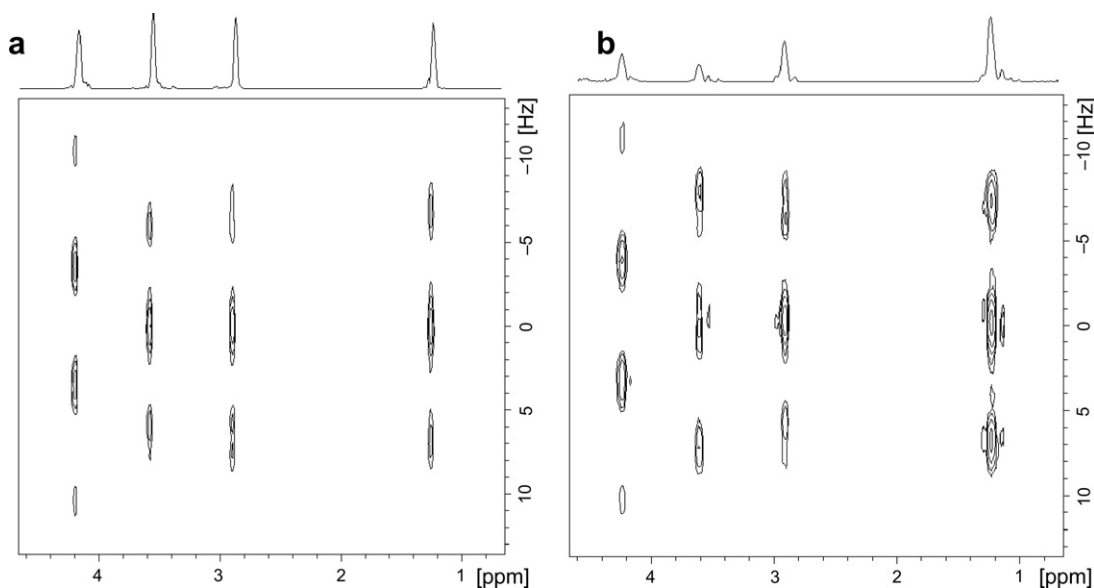


Fig. 2. Comparison between ultrafast 500 MHz  $J$ -resolved spectra acquired on a  $100 \text{ mmol l}^{-1}$  3-ethyl bromopropionate sample in  $\text{CDCl}_3$  at 298 K. Both spectra were obtained in 500 ms, with the same average excitation time  $T_e = 60$  ms. Spectra obtained with Pelupessy's encoding scheme (a) or Tal's encoding scheme using inverted  $G_e^\pi$  gradient (b). Both spectra were processed with the same apodization function and post processing parameters, as described in Section 4.

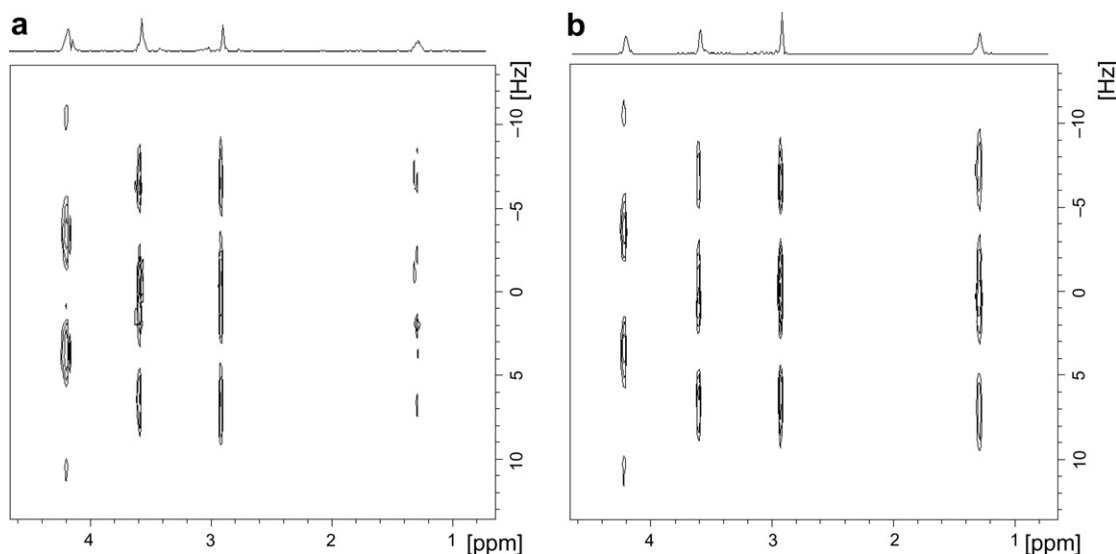


Fig. 3. 500 MHz ultrafast  $J$ -resolved spectra obtained acquired on a  $100 \text{ mmol l}^{-1}$  3-ethyl bromopropionate sample in  $\text{CDCl}_3$  at 298 K. Both spectra were obtained in 500 ms, with the same average excitation time  $T_e = 120 \text{ ms}$ . (a) Spectrum obtained with Pelupessy's encoding scheme consisting of two 60 ms  $180^\circ$  pulses. (b) Spectrum obtained with multi-echo excitation scheme formed by six 20 ms  $180^\circ$  pulses. Both spectra were processed with the same apodization function and post processing parameters, as described in Section 4.

The aforementioned effects may be due to molecular diffusion or transverse relaxation. However, we measured the transverse relaxation times of 3-ethyl bromopropionate and values between 0.4 and 1.5 s were obtained, which is much higher than the duration of the excitation period. The maximum magnetization decrease at the end of the 120 ms excitation period is only 26% for  $T_2 = 0.4 \text{ s}$ , which clearly indicates that transverse relaxation is not the main cause of sensitivity decrease. Moreover, the same spectrum was obtained in a more viscous solvent ( $\text{DMSO-}d_6$ ) in order to limit diffusion effects. The  $S/N$  ratio was increased by a factor of 2, which confirms that diffusion is the main reason that could explain the  $S/N$  ratio decrease previously described. In spite of the good results obtained in  $\text{DMSO-}d_6$ , we chose to keep using  $\text{CDCl}_3$  as a solvent for the continuation of our study, as in practice it is not always possible to choose a viscous solvent.

To evaluate the effect of diffusion for another pulse sequence, we also performed ultrafast TOCSY experiments on 3-ethyl bromopropionate in  $\text{CDCl}_3$ , with  $T_e = 60$  and 120 ms.  $S/N$  for cross-peaks was decreased from  $23 \pm 1$  to  $16 \pm 2$ , which shows that diffusion effects occur even when a mixing period is present. A more general, theoretical and quantitative analysis of diffusion losses will be given in an ulterior paper.

$J$ -resolved experiments performed with different excitation gradient amplitudes showed important  $S/N$  decrease when increasing  $G_e^x$  values, which also confirms the influence of molecular diffusion. Consequently, the first possibility to limit diffusion effects in pulse sequences with long  $T_e$  values is to use weaker gradient amplitudes. However, all the spectra presented above were already obtained with the smallest amplitudes available on our spectrometer, as they were only 2% of their maximum strength. Lower

values would lead to important signal distortions. As a consequence, it appears necessary to propose an excitation scheme designed to limit diffusion effects when a high  $T_e$  is required to obtain a good resolution. To achieve this, we propose a multi-echo encoding pattern which is described in Fig. 1d. In this pulse sequence based on Pelupessy's technique [11], the two  $180^\circ$  chirp pulses are replaced by a succession of shorter  $180^\circ$  pulses pairs applied during alternated gradients. The duration of  $180^\circ$  pulses is given by  $T_e/(2n)$ , where  $2n$  is the number of echoes. For identical  $T_e$  values, theoretical spatial encoding level and resolution are the same as in Pelupessy's scheme, but diffusion effects should be reduced because shorter gradients are employed [15,16].

The application of this multi-echo pattern is presented in Fig. 3b, for a 6 echo scheme with 20 ms pulses, leading to a total  $T_e$  of 120 ms. The resolution is the same ( $\Delta\nu^{1/2} = 13 \pm 1 \text{ Hz}$ ) as for Pelupessy's pulse sequence with  $T_e = 120 \text{ ms}$  (Fig. 3a). Moreover, sensitivity has been increased by a factor of 2 ( $S/N = 30 \pm 8$  for the highest peak of the quadruplet) and all peaks are now well defined. This shows the efficiency of multi-echo excitation to limit diffusion effects.

In order to further improve sensitivity, we tried to use more than 6 echoes while keeping  $T_e$  unchanged. However, it did neither increase nor decrease  $S/N$  ratio. Moreover, experiments performed at different  $T_e$  values showed that multi-echo excitation leads to sensitivity and resolution losses when  $T_e$  is too small, i.e. when diffusion is not predominant. This unexpected negative effect could be due to adiabaticity losses when  $180^\circ$  pulse durations become shorter, since the adiabaticity factor is directly proportional to the pulse duration [17]. These observations underline the limits of the multi-echo method that should be



applied with care. In order to choose the experimental parameters for a given excitation scheme, the minimum adiabaticity factor reached during the pulse could be calculated according to [17].

Finally, as suggested in [12], we also tried to combine Tal's and Pelulessy's excitation schemes, however resolution and  $S/N$  improvements were less significant than the ones obtained by multi-echo excitation pattern based on Pelulessy's scheme.

### 3. Conclusion

The comparison between different continuous encoding schemes leads to the conclusion that Tal's encoding scheme with inverted gradient is as efficient as Pelulessy's concerning resolution aspects. Based on Pelulessy's technique, the new multi-echo encoding scheme presented above offers the possibility of acquiring 2D ultrafast spectra with good resolution while limiting sensitivity losses due to molecular diffusion. It is applied to  $J$ -resolved spectroscopy but might be useful for other single-scan  $nD$  experiments.

As a conclusion, we may define the best conditions for acquiring high-resolution ultrafast 2D spectra: high  $T_e$  value compensated by multi-echo excitation, small gradient amplitudes and viscous solvent when it is possible. The temperature effects should also be taken into consideration.

Another important aspect of ultrafast  $J$ -resolved spectroscopy is the influence of homonuclear  $J$ -couplings on peak intensities, which was not considered in this work. A detailed analysis of this aspect will be given elsewhere.

Resolution improvements of ultrafast spectra could progressively lead to the replacement of conventional techniques by ultrafast methods in a wide range of applications, from structural analysis to *in vivo* spectroscopy. The use of such techniques for quantitative analysis [18] will be considered in later works. However, it should be kept in mind that in spite of the improvements presented here, ultrafast acquisition can be used only when sufficient  $S/N$  is available [19], which could be a problem at low concentrations.

### 4. Experimental

In order to obtain a  $100 \text{ mmol l}^{-1}$  solution,  $13.0 \mu\text{l}$  of 3-ethyl bromopropionate, purchased from Sigma Aldrich, were dissolved in 1 ml of  $\text{CDCl}_3$  or 1 ml of  $\text{DMSO-}d_6$ . After homogenization, each sample was filtered and analysed in a 5 mm tube.

NMR spectra were recorded at 298 K on a Bruker Avance 500 DRX spectrometer, at a frequency of 500.13 MHz with a triple resonance TBI probe including  $z$ -axis gradient.

Ultrafast 2D  $J$ -resolved spectra were obtained with  $\pm 1.1 \text{ G cm}^{-1}$  excitation gradients and Wurst-8 pulses [20] with a sweep range of 9.4 kHz. For Tal's inverted scheme, the  $\pi/2$  pulse, applied for 60 ms, was carefully calibrated to obtain an accurate  $90^\circ$  excitation with an adiabaticity

parameter of 0.068 [14]. It was followed by a  $\pi$  Wurst-8 adiabatic pulse applied for 30 ms. For Pelulessy's encoding scheme, Wurst-8 adiabatic pulses [20] were applied for 30 ms for  $T_e = 60 \text{ ms}$ , or for 60 ms for  $T_e = 120 \text{ ms}$ . The same pulses were used for multi-echo encoding, with durations depending on  $T_e$  and number of echoes.

The  $J$ -resolved detection block was formed of 64 detection gradients of duration  $T_a = 6.9 \text{ ms}$  each and a strength  $G_a$  adapted to observe the relevant chemical shift range during  $T_a$ . For each experiment, the gradient  $G_c$ , applied during  $500 \mu\text{s}$ , was set to adjust the centre of the chemical shift range in the middle of the acquisition window.

For TOCSY [21] spectra, the same excitation block as for  $J$ -resolved spectra was used, followed by a 80 ms DIPSI-2 [22] mixing period. The detection block was formed of 128 alternated detection gradients of duration  $T_a = 280 \mu\text{s}$  each with a strength  $G_a$  adapted to observe the relevant chemical shift range.

All spectra were processed in the same way: zero-filling once and shifted square sine-bell apodization functions in  $v_2$  dimension. All ultrafast spectra were subjected to noise subtraction along the  $k/v_1$  axis, but  $S/N$  and resolution measurements were performed before this operation.

All spectra were analysed using the Bruker program Topspin 2.0. The specific processing for ultrafast spectra was performed using our home-written routine in Topspin.  $S/N$  ratios and  $\Delta v^{1/2}$  are average values determined on five successive experiments.

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